# Post-Quantum Zero-Knowledge and Signatures from Symmetric-Key Primitives

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Digital Signatures in a post-quantum world

• RSA and DLOG based schemes insecure

New schemes

- based on new structured hardness assumptions (lattices, codes, isogenies, etc.)
- based on symmetric primitives: Hash-based signatures

Other alternatives only relying on symmetric primitives?

Recent years progress in two areas

- Symmetric-key primitives with few multiplications
- Practical ZK-Proof systems over general circuits

New signature schemes based on these advances

### **Digital Signatures**



Existential Unforgeability under Chosen-Message Attacks

- Adversary may see signatures on arbitrary messages
- Still intractable to output signature for new message

#### Three move protocol:



- Important that *e* unpredictable before sending *a*
- aka (Interactive) Honest-Verifier Zero-Knowledge Proofs

Non-interactive variant via Fiat-Shamir [FS86] transform

#### Well known methodology

One-way function  $f_k: D \to R$  with  $k \in K$ 

- $\cdot sk \stackrel{\scriptscriptstyle R}{\leftarrow} K$
- $\cdot y \leftarrow f_{sk}(x), pk \leftarrow (x, y)$

Signature

- $\Sigma$ -protocol to prove knowledge of sk so that  $y = f_{sk}(x)$
- Use Fiat-Shamir transform to bind message to proof  $e \leftarrow H(a \| m)$

# ZKBoo [GMO16]

#### Efficient $\Sigma$ -protocols for arithmetic circuits

• generalization, simplification, + implementation of "MPC-in-the-head" [IKOS07]

Idea

- 1. (2,3)-decompose circuit into three shares
- 2. Revealing 2 parts reveals no information
- 3. Evaluate decomposed circuit per share
- 4. Commit to each evaluation
- 5. Challenger requests to open 2 of 3
- 6. Verifies consistency

Efficiency

• Heavily depends on #multiplications



Improved version of ZKBoo:

- Remove redundant information from views
- Remove redundant checks
- Proof size reduction to less than half the size
- But without extra computational cost

Optimization 1: Share Function and Input Shares

- Use PRNGs  $R_i$  keyed with  $k_i$
- $\cdot$  Share as  $x_1 \leftarrow R_1(0), x_2 \leftarrow R_2(0)$  and  $x_3 \leftarrow x x_1 x_2$
- $x_1$  and  $x_2$  deterministically computable by the verifier from  $k_1$  and  $k_2$
- Only need to include  $k_i$  in View<sub>1</sub> and View<sub>2</sub>
- Expected proof size reduction:  $4r \cdot |x|/3$  bits

Optimization 2: Not Including Commitments

- For opened views, verifier can re-compute commitment
- $\cdot$  Only one commitment needs to be sent
- View *e* as a "commitment to the commitments"
- Proof size reduction:  $2r \cdot |c|$  bits

Optimization 3: Not Including the Output Shares

- Output shares  $y_i$  for opened views can be re-computed
- Third output share reconstructable from *y* and re-computed output shares
- Unnecessary to include any output shares in proof
- Proof size reduction:  $3r \cdot |y|$  bits

Optimization 4: No Additional Randomness for Commitments

- First input to the commitment is seed  $k_i$
- Protocol input to commitment doubles as randomization values
- No additional randomness for commitments necessary
- ROM is needed here, but we already need it for non-interactivity

Optimization 5: Not Including Viewe

- Verifier can re-compute View<sub>e</sub> given k<sub>e</sub>, k<sub>e+1</sub> and wire values of View<sub>e+1</sub>
- By binding of the commitment, commitment verifies only if View<sub>e</sub> re-computed correctly
- · Only need to store input wires of  $\operatorname{View}_e$
- Proof size reduction:  $r \cdot |View|$  bits

Substitution-permutation-network design

- Very lightweight S-box with one AND gate per bit
- S-box layer is only partial
- Very expensive affine layer with n/2 XOR gates per bit.
- Allows selection of instances minimizing, e.g.
  - ANDdepth,
  - number of ANDs, or
  - ANDs / bit

Blocksize	S-boxes	Keysize	Data ANDdepth		# of ANDs	ANDs/bit
n	m	k	d	r		
256	2	256	256	232	1392	5.44
512	66	256	256	18	3564	6.96
1024	10	256	256	103	3090	3.02

Table 1: LOWMC parameters for 128-bit PQ-security

#### Fish:

- Turn ZKB++ and OWF into signature scheme
- via Fiat-Shamir Transform
- Instantiate OWF with LowMC v2
- $\cdot$   $\Rightarrow$  EUF-CMA security in the ROM

Proving Fiat-Shamir transform secure in QROM faces problems

- Proof requires rewinding
- Unclear how to translate

Use Unruh Transform [Unr15]

Take random permutation G and random oracle H

- Produce multiple proofs (*c<sub>i</sub>*, *G*(*resp<sub>i,1</sub>*), ... , *G*(*resp<sub>i,1</sub>*))
- Hash all of them with *H*
- Use the result of hashing to indicate which response of each *c<sub>i</sub>* should be revealed

#### Picnic:

- Turn ZKB++ and OWF into signature scheme
- via Unruh Transform
- Instantiate OWF with LowMC v2
- $\cdot$   $\Rightarrow$  EUF-CMA security in the QROM

Unruh Transform incurs overhead in signature size

• But careful tweaking reduces overhead to factor 1.6

- Recall: OWF  $f_k : D \to R$ ,  $sk \leftarrow K$ ,  $pk \leftarrow (x, f_{sk}(x))$
- Security parameter  $\kappa$

OWF represented by arithmetic circuit with

- $\cdot$  ring size  $\lambda$
- $\cdot$  multiplication count a

Signature size:  $|\sigma| = c_1 + c_2 \cdot (c_3 + \lambda \cdot a)$  where  $c_i$  are polynomial in  $\kappa$ 

## **OWF with few multiplications?**

#### Build OWF from

name	security	$\lambda \cdot a$	
AES	128	5440	$\mathbb{F}_2$ approach
AES	128	4000?	. <b>₽<sub>24</sub> approach</b>
AES	256	7616	$\mathbb{F}_2$ approach
SHA-2	256	> 25000	
SHA-3	256	38400	
Noekeon	128	2048	
Trivium	80	1536	
PRINCE		1920	
Fantomas	128	2112	
LowMC v2	128	< 800	
LowMC v2	256	< 1400	
Kreyvium	128	1536	
FLIP	128	> 100000	
MIMC	128	10337	
MIMC	256	41349	

name	security	$ \sigma $
AES	128	339998
AES	256	473149
SHA-2	256	1331629
SHA-3	256	2158573
LowMC v2	256	108013

#### **Example of Exploration of Variation of LowMC Instances**



Figure 1: Measurements for instance selection (128-bit PQ-security).

Scheme	Gen	Sign	Verify	sk	pk	$ \sigma $	М
Fish-10-38	0.01	29.73	17.46	32	32/64	116 <i>K</i>	ROM
Picnic-10-38	0.01	31.31	16.30	32	32/64	191 <i>K</i>	QROM
MQ 5pass	1.0	7.2	5.0	32	74	40 <i>K</i>	ROM
SPHINCS-256	0.8	1.0	0.6	1 <i>K</i>	1 <i>K</i>	40 <i>K</i>	SM
BLISS-I	44	0.1	0.1	2K	7 <i>K</i>	5.6 <i>K</i>	ROM
Ring-TESLA	17 <i>K</i>	0.1	0.1	12 <i>K</i>	8 <i>K</i>	1.5 <i>K</i>	ROM
TESLA-768	49 <i>K</i>	0.6	0.4	3.1 <i>M</i>	4 <i>M</i>	2.3 <i>K</i>	(Q)ROM
FS-Véron	n/a	n/a	n/a	32	160	≥ 126 <i>K</i>	ROM
SIDHp751	16	7 <i>K</i>	5 <i>K</i>	48	768	138 <i>K</i>	QROM

Table 2: Timings (ms) and key/signature sizes (bytes)

- ZKB++: Improved ZK proofs for arithmetic circuits
- **Fish**/ **Picnic**: Two new efficient post-quantum signature schemes in ROM and QROM
- Applications beyond signatures: NIZK proof system for arithmetic circuits in post-quantum setting

#### **Outlook and Future Work**

- Alternative symmetric primitives with few multiplications
  - Something new with even less multiplications than LOWMC?
  - 256-bit secure variant of Trivium/Kreyvium?
- More LowMC cryptanalysis
  - More aggressive LOWMC parameters with very low allowable data complexity, e.g. only 2 plaintexts.
- Analysis regarding side-channels
- Unruh Transform with constant overhead?

# Thank you.

- Preprint will soon appear on eprint.
  - Merge of https://ia.cr/2016/1085 and https://ia.cr/2016/1110.



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